MICROWAVE RADAR METEOROLOGY Foundations and Applications





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F.S. Marzane – Microwave Radar Meteorology: foundations and applications

RAINFALL FORECAST A conceptual diagram



RAINFALL SENSING Points of view



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RADAR METEOROLOGY Lecture's contents

Radar sensor

- Pulsed, Doppler, and polarimetric systems
- Receiver sensitivity, antenna specifications and radar volume resolution

Radar equation

- Atmospheric refraction and attenuation
- Radar equation for single and distributed scatterers

Radar signal

- Signal statistics and decorrelation
- Noise reduction techniques

Radar applications

- Clouds and precipitation
- Rainfall backscattering and polarimetric measurables

Radar products

- Radar measurements and error budget
- Examples of radar measurements and estimates

RADAR METEOROLOGY Historical perspective

Radio era

- 1886: H. Hertz experiments e.m. wave reflection
- 1902: G. Marconi carries out radio-propagation experiments
- 1922: object detection with continuous wave instruments
- 1932: object detection with pulsed wave instruments

Radar era

- 1938: construction of radars for aircraft detection and ranging
- 1941: first use of radars for cloud observations
- 1960s: use of radars for quantitative rainfall estimation
- 1970s: use of Doppler radars at VHF-UHF for turbulence and wind

Computer era

- 1980s: impact of computers on data acquisition and processing
- 1990s: use of digital receivers and pulse forming
- 1990s: use of radars for weather nowcasting
- 2000s: spaceborne radars and sensors' synergy

RADAR METEOROLOGY Context and objectives

Radar (RAdio Detection and Ranging)

- Pulsed incoherent and coherent radars (Doppler or MTI)
- Continuous-wave and frequency modulation (FM-CW)

Meteorological radars

- Rain (weather) radars: rainfall monitoring from ground and space
- Cloud radars: cloud monitoring from ground and space
- Stratosphere-Troposphere (ST) radars: wind profiling from ground

Weather (rain) radars

- Monitoring of three-dimensional (3-D) structure of rainfall and winds
 - Covering large areas (100-400 km) around ground site
 - Measuring of e.m. backscattering due to cloud hydrometeor volumes
- Advantages with respect to:
 - optical sensors (e.g, higher penetration, any meteo condition)
 - radiometers (e.g., ranging capability,)
 - rain-gauges (e.g., larger effective coverage, rain structure)
- Disadvantages: high power, complexity, maintenance

RADAR METEOROLOGY A system approach



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RADAR SENSOR Pulsed microwave systems

Principle

- Send a train of short, high-power pulse of e.m. energy at high frequency (GHz)
- E.m. energy, captured by atmospheric objects, is partially absorbed and reirradiated (scattered) into many directions among which that of radar (backscattered: radar echo)
- Angular resolution: derived from the antenna pointing direction and limited by its beam width
- Range resolution: derived from the twoway time employed by radar pulse echo (antenna-object-antenna) and depending by medium light velocity

Legenda

- PRF: Pulse Repetition Frequency
- RF: Radio Frequency (f₀)
- PP: Peak-to-peak power
- P_t: Peak power of the transmitter



RADAR SENSOR Principle of pulsed systems





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RADAR SENSOR Pulsed incoherent scheme



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RADAR SENSOR Pulsed incoherent system

device which determines the form e repetition of RF pulse

band-pass amplifier and filter for noise reduction of IF signal

device which mixes RF signal with LO doing amplification and filtering

microwave tube (magnetron or klystron amplifier)

device which controls mixer frequency

detector of IF envelope power at baseband

3-port circulator which separates TX from RX signal

Radar components

- Master oscillator (MO): system reference oscillator
- Modulator:
- Power oscillator:
- **Duplexer**:
- Local oscillator (LO):
- Mixer:
- **Amplifier:**
- Video detector:
- Signal processing

 $s_{RF}(t) = \left[A\cos(2\pi f_0 t)\right]rect(f_r t)$ $x_{RF}(t) = a(t) \cos \left[2\pi f_0 t + \varphi(t)\right]$ $x_{mix}(t) = a(t) \cos \left[2\pi f_0 t + \varphi(t) \right] \left\{ b \cos \left[2\pi (f_0 + f_c) t \right] \right\}$ $x_{IF}(t) = \frac{a(t)b}{2} \cos \left[2\pi f_c t + \varphi(t)\right] = a'(t) \cos \left[2\pi f_c t + \varphi(t)\right]$ $x_{BB}(t) = |x_{IF}(t)|^2 = |a'(t)|^2$

Transmitted Radio Frequency (i.e., GHz)

Received Radio Frequency

Mixer signals

Intermediate Frequency (i.e., MHz)

Base-band signal (i.e., kHz)

RADAR SENSOR Doppler frequency shift



(a) Stationary source







If leaving target: $\theta < \pi/2 \implies f_d < 0$ If approaching target: $\theta > \pi/2 \implies f_d > 0$

Monostatic Radar

- **Twice a Doppler frequency shift**
- from radar to target
- from target to radar

$$f_{RF} = f_0 + f_d$$









RADAR SENSOR Pulsed coherent scheme

Per poter determinare la velocità Doppler del bersaglio puntiforme devo usare un

RICEVITORE COERENTE



RADAR SENSOR Pulsed coherent scheme



RADAR SENSOR Pulsed coherent scheme

• L'atmosfera è un bersaglio distribuito, ossia è costituita da un elevato numero di bersagli elementari (idrometeore)

• L'eco radar è la somma di tanti contributi elementari del tipo visto in precedenza (impulso rettangolare a RF)



RADAR SENSOR Pulsed coherent system



L'eco ricevuto all'istante t0 è la somma dei contributi di tutti i bersagli elementari che si trovano ad una distanza dal radar compresa tra $c \cdot (t_0 - \tau)/2$ e $c \cdot t_0/2$

Il segnale ricevuto viene prima campionato (nel GPM-500C con una frequenza di 2.4 MHz, ossia ogni 417 ns) e quindi i campioni vengono processati.

Ogni campione è rappresentativo di un volume elementare (tronco di cono) con altezza pari a $(c \cdot \tau)/2$

RADAR SENSOR Pulsed coherent system

Detection of received signal phase

$$\varphi(t) = -2\left[\frac{2\pi}{\lambda}r(t)\right] \Rightarrow \frac{d\varphi(t)}{dt} \equiv -\frac{4\pi}{\lambda}\frac{dr(t)}{dt} = -\frac{4\pi}{\lambda}u_r(t) \equiv 2\pi f_d(t) \Rightarrow f_d(t) = -\frac{2}{\lambda}u_r(t)$$

Signal processing

$$\begin{split} s_{RF}(t) &= [A\cos(2\pi(f_0 + f_c)t)]rect(f_r t) = [A\cos(2\pi f_0't)]rect(f_r t) \\ x_{RF}(t) &= a(t)\cos[2\pi f_0 t + \varphi(t)] = a(t)\cos\left[2\pi f_0 t - \frac{2\pi}{\lambda}2r(t)\right] \\ x_{mix}(t) &= a(t)\cos[2\pi(f_0 + f_c)t + \varphi(t)] \left\{b\cos[2\pi f_0 t]\right\} \\ x_{IF}(t) &= a'(t)\cos[2\pi f_c t + \varphi(t)] = a'(t)\cos[\varphi(t)]\cos(2\pi f_c t) - a'(t)\sin[\varphi(t)]\sin(2\pi f_c t) \\ x_{IF}(t) &\equiv I(t)\cos(2\pi f_c t) - Q(t)\sin(2\pi f_c t) = \operatorname{Re}\left\{I(t) + jQ(t)\right]e^{j2\pi f_c t}\right\} = \operatorname{Re}\left\{a'(t)e^{j\varphi t(t)}\right]e^{j2\pi f_c t}\right\} \\ x_{BB}(t) &= \begin{cases}I(t) &= a'(t)\cos[\varphi(t)] \\ Q(t) &= a'(t)\sin[\varphi(t)] \end{cases} \text{ with } V(t) = I(t) + jQ(t) \end{split}$$

RADAR SENSOR Doppler velocity ambiguity

Signal sampling (Shannon) theorem

 A signal with a finite energy (a maximum spectral frequency f_M) is reconstructed from its temporal samples if the sampling frequency f_s:

$$f_M \ge \frac{f_s}{2} \implies T_M \le \frac{T_s}{2}$$

- Unambiguous Doppler frequency
 - If maximum frequency is f_r:

$$f_d \ge f_{d\max} = \frac{f_r}{2} \implies u_{r\max} = \pm f_r \frac{\lambda}{4}$$

Velocity-range limit

$$u_{r\max}r_{\max} = [(f_r\lambda)/4][cT_c)/2] = (c\lambda)/8$$

Ambiguity reduction techniques

- Doppler phase measured between 2 pulses
- Dual-PRF: double of unanmbiguos fd
- Phase and polarization pulse coding





RADAR SENSOR Issues on coherent systems

Microwave transmitter

- MAGNETRON: self-oscillating microwave tube with cylindrical structure (cross-field device), able to handle high power (up to 2000 kW peak). A high (up to 50 kV) DC voltage is applied to coaxial cathode (+) and anode (-) together with a static magnetic high field (up to 1 A/m). The emitted electron beam is spatially modulated (bunches) and output is coupled into one of ring resonant cavities. The latter determines the radio-frequency (RF) signal. Oscillation condition is governed by Hartree's curve. Overall efficiency is about 50%.
 - When input voltage is pulsed (as in radars), no inter-pulse coeherence is guaranteed (even though phase information may be retained by injecting a CW signal).
- **KLYSTRON:** microwave-tube amplifier with a linear (linear-field) structure, able to handle medium power (up to 1000 kW). An electron beam is formed by an electron gun (thermoionic emission by cathode-anode at > 1000 K), passes trhough 2 or more resonant cavities in succession and is collected on a collector. Electric field of first cavity gaps induce electron bunches whose are "focused" on (load) resonant cavities which produce output RF signal.
 - Within pulsed radars, klystron is used as an amplifier excited by a local microwave oscillator. These scheme guarantees a high phase purity (low phase noise) and an inter-pulse coherence.

Base-band detection

- **Amplitude:** logarithmic detector in order to deal with large amplitude (i.e., *a'(t)*) dynamics.
- **Phase**: linear detector to extract in-phase I(t) and quadrature Q(t) components

RADAR SENSOR E.m. wave polarization

Polarization states



Horizontal Polarization

Curve described in 3-D space by the free end of the monochromatic wave vector

- Horizontal H (w.r.t. ground)
- Vertical V
- Circular (LHC, RHC)

Linear polarizations

 $\underline{E}(r,t) = \underline{E}_{0p}(t) \cos[2\pi f_0 t + \varphi(t)]$ $\underline{E}_{0v}(t) = E_{0v}(t)\hat{\underline{z}}$

 $\underline{E}_{0h}(t) = E_{0h}(t)\underline{\hat{x}}$



RADAR SENSOR Issues on polarimetric radars

Configuration

- Alternate transmission
 - Single-transmitter and single-receiver
 - Alternate transmission between H and V fields
 - 1 Single receiver
 - 1 Anomalous propagation removal
 - Polarization switching
 - ↓ H and V non-contemporary data
- Simultaneous transmission
 - Single transmistter and dual receiver
 - Simultaneous transmission of H and V fields
 - 1 No polarization switching (costly and loss)
 - No delay in H and V acquisition data
 - **Fast scanning (half time w.r.t. alternate trans.)**
 - Cross-polarization effects in received data
 - **Dual receiver and limitation in polarimetric features**

Receiver

- Digital receiver at IF stage
 - Sampling of IF signal (A/D digitizers)
 - Digital processing of binary I/Q sequences





RADAR SENSOR Alternate polarim. system



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RADAR SENSOR Simultaneous polarim. system



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RADAR SENSOR Receiver sensitivity

Noise sources

- cosmic, artificial (human) and atmospheric emission (H₂0, 0₂ at MW)
- internal, due to electron thermal mobility (white Gaussian noise at MW).

Internal noise of receiver

- Receiver input power with a resistance load at T_0 and bandwith B_n : $N_i = kT_0B_n$
- Noise figure F_n or equivalent noise temperature $T_e: T_e = T_0(F_n I)$

$$N_{i} = kT_{0}B_{n} \longrightarrow \textbf{Radar receiver} \longrightarrow N_{0} = \textbf{F}_{n}(GN_{i}) = k(T_{0} + \textbf{T}_{e})B_{n}$$
$$S_{i} \longrightarrow S_{0} = GS_{i}$$

Minimum detectable signal

Minimum signal detectable over the noise receiver (e.g., -110 dBm = 10⁻¹¹ mW)

$$F_n = \frac{S_i / N_i}{S_0 / N_0} \implies S_{iMin} = F_n N_i \frac{S_0}{N_0} \Big|_{Min} = F_n (kT_0 B_n) \frac{S_0}{N_0} \Big|_{Min}$$

• Matched filters to increase S/N: for square pulses. $B_n \approx 1/\tau$ and triangular shape

RADAR SENSOR Aperture antenna basics

Radar antennas

- Parabolic reflector antenna
- Prime-focus feeder (horn)
- Optional radome protection
- Optional polarization capability
- Antenna radiation
 - Radiation pattern function

$$f(\theta, \varphi) = FFT[E_a(x, y)]$$

Irradiated eletric far-field (for r≥L²/λ)

$$E(r,\theta,\varphi) = E_0 f(\theta,\varphi) \frac{e^{-jkr}}{r}$$

Power flux density [W/m²]

$$P(r,\theta,\varphi) = \frac{1}{2\eta_0} \left| E(r,\theta,\varphi) \right|^2 = \frac{E_0}{2\eta_0 r^2} \left| f(\theta,\varphi) \right|^2$$



RADAR SENSOR Antenna parameters

Directivity and Gain

$$D(\theta,\varphi) = \frac{P(r,\theta,\varphi)}{W_T / 4\pi r^2} = \frac{\left|f(\theta,\varphi)\right|^2}{W_T / 4\pi}, \quad G(\theta,\varphi) = \eta_r D(\theta,\varphi)$$

Effective area

$$A_e(\theta,\varphi) = \frac{W_R}{P_i(r,\theta,\varphi)} = \frac{\lambda^2}{4\pi} D(\theta,\varphi) = D_M \left| f_n(\theta,\varphi) \right|^2$$

Beamwidth (reflector antennas)

$$\left|f_{n}(\Theta_{3dB}/2,\varphi)\right|^{2} = 0.5 \implies \Theta_{3dB} \cong 70\frac{\lambda}{L}, \ D_{M} \cong \frac{4\pi}{(\Theta_{3dB})^{2}}$$

Polarization capability

- Ortho-Mode Transducer (H/V) at horn feeder
- Low sidelobes (<30 dB) similar for H/V patterns
- Isolation between H/V patterns (no cross-pol.)
 - Azimuthally symmetric radiation pattern at H/V
- Effects of supporting struts and radome paneling



RADAR SENSOR Antenna parameters

Example: Radar GPM-500C

Cassegrain dual-offset

- fascio di 0.9° (a -3 dB)
- velocità max 30 deg/s
- lobi secondari molto bassi
- ottima simmetria tra H e V



RADAR SENSOR Antenna diagram

Example: Radar GPM-500C

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- fascio di 0.9° (a -3 dB)
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RADAR SENSOR Volume resolution



RADAR SENSOR Volume resolution

Spatial resolution

- Capability of discriminating 2 objects in space (range, zenith and azimuth in spherical coordinates)
- **Radial resolution** \geq
 - **Resolution in range:**

$$\Delta r = \frac{c \tau}{2}$$

- ${\it P}_{3dB}$ $\widehat{\boldsymbol{\varTheta}}_{3dB}$ Matched receivers have a lower radial resolution
- Use of pulse compression to increase spatial res.
- Transverse resolution
 - $\Delta \Omega = \frac{\Delta S}{r^2} \implies \Delta S = r^2 \Delta \Omega \cong r^2 \Omega_{3dB}$ • Resolution in zenith-azimuth:
 - Affected by side lobes contribution.

Pulse volume resolution

$$V_{bin} = \Delta r \Delta S = (c \tau/2) r^2 \Omega_{3dB} \cong \frac{\pi}{4} (c \tau/2) r^2 \Theta_{3dB} \Phi_{3dB}$$

- Volume varies with range (for 1° and 1 μ s, at 100 km Δ r=150 m and Δ S=1745² m²)
 - Energy volume distribution can be not uniform in range (e.g., matched filters) and in transverse direction (e.g., directivity angular variation)



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Radar equation

- Atmospheric refraction and attenuation
- Radar equation for single and distributed scatterers
- Radar signal
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Radar applications

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RADAR EQUATION Atmospheric refraction

Ζ.

Atmospheric refractivity

• Refractive index:

$$n = \frac{c}{v} = \sqrt{\varepsilon_r} = n' - jn''$$

Refractivity:

$$N = (n'-1)10^{6} = f(p/T, e/T^{2})$$

- Optical rays
 - Geometrical optics equation:

$$\frac{1}{\rho} = \frac{10^6}{n} \frac{dN}{dz} \cos\beta, \quad N(z) = N_0 e^{-z/H}$$

with ρ ray curvature.

- If standard atmosphere, dN/dz=-40 [N/km]
 - Earth effect. radius $R_e = 4/3R_T = 4/3(6370) = 8500$
 - Rays are rectilinear and Earth flatter

Specific attenuation

• For two-way path, the attenuation factor L:

$$dW = -2\alpha W dr \implies W(r) = W_0 e^{-2\int_0^r \alpha dr} = W_0 L^2(r)$$





► X

Power flux density upon scatterer

$$P_i(r,\theta,\varphi) = \frac{W_T}{4\pi r^2} G_M \left| f_n(\theta,\varphi) \right|^2 L(r)$$

Backscattering radar cross section

$$\sigma_b(-\theta,-\varphi,\theta,\varphi) = 4\pi r^2 \frac{P_r(r,\theta,\varphi)}{P_i(r,\theta,\varphi)}$$

Received power

$$P_r(r,\theta,\varphi) = \frac{\sigma_b}{4\pi r^2} P_i = \frac{\sigma_b}{4\pi r^2} L \frac{W_T}{4\pi r^2} G_M \left| f_n(\theta,\varphi) \right|^2 L \implies W_R = A_e P_r = \frac{\lambda^2}{4\pi} G P_r$$

Radar equation for a single scatterer

$$W_{R} = \left(\frac{W_{T}G_{M}^{2}|f_{n}(\theta,\varphi)|^{4}\lambda^{2}}{(4\pi)^{3}}\right)\sigma_{b}\frac{L^{2}}{r^{4}} = \left(\frac{W_{T}\eta_{r}^{2}A_{e}^{2}}{4\pi r\lambda^{2}}\right)\sigma_{b}\frac{L^{2}}{r^{4}} \implies W_{R} = C_{1}L^{2}\frac{\sigma_{b}}{r^{4}}$$

• For a point target, $f_n=1$ and $W_{R} \approx 1/r^4$. Constant C_1 depends on radar specs.



RADAR EQUATION Effect of distributed scatterer

Distributed scatterers

- Set of a large number N_{part} of equal-size scatterers, simultaneously present in the same resolution volume V_{bin} with randomly distrubuted phase and totally filling the volume (e.g. raindrops).
- Volumetric reflectivity [m⁻¹]

$$\eta = \left(\frac{\sum_{i=1}^{N_{part}} \sigma_{bi}}{dV}\right) \implies \sum_{i=1}^{N_{part}} \sigma_{bi} = dV \left(\frac{\sum_{i=1}^{N_{part}} \sigma_{bi}}{dV}\right) = dV\eta$$

Particle and total received power

$$dW_{Ri} = \left(\frac{W_T G_M^2 \lambda^2}{(4\pi)^3}\right) \frac{\left|f_n(\theta, \varphi)\right|^4}{r_i^4} \sigma_{bi} = C \frac{\left|f_n(\theta, \varphi)\right|^4}{r_i^4} L^2 \sigma_{bi}$$

$$dW_R = \sum_{i=1}^{N_{part}} dW_{Ri} = \sum_{i=1}^{N_{part}} C \frac{\left|f_n(\theta, \varphi)\right|^4}{r_i^4} L^2 \sigma_{bi} \cong C \frac{\left|f_n(\theta, \varphi)\right|^4}{r^4} L^2 \sum_{i=1}^{N_{part}} \sigma_{bi} \frac{dV}{dV} \cong C \frac{\left|f_n(\theta, \varphi)\right|^4}{r^4} L^2 \eta dV$$

$$W_{Rtot} = \int_{V_{bin}} dW_R = \int_V C \frac{\left|f_n(\theta, \varphi)\right|^4}{r^4} L^2 \eta dV \equiv \langle W_R \rangle$$


RADAR EQUATION Distributed scatterer form

 $W_T G_M$

Distributed scatterers

 Set of a large number of scatterers, simultaneously present in the same resolution volume V_{bin} with randomly distrubuted phase and totally filling the volume (e.g. raindrops).

> Total (average) received power

$$< W_R >= \left(\frac{W_T G_M^2 \lambda^2}{(4\pi)^3}\right) L^2 \int_{V_{bin}} \frac{\left|f_n(\theta, \varphi)\right|^4}{r^4} \eta dV = \left(\frac{W_T G_M^2 \lambda^2}{(4\pi)^3}\right) L^2 \eta \Delta r \int_{V_{bin}} \frac{\left|f_n(\theta, \varphi)\right|^4}{r^2} d\Omega$$

where $dV = dr(r^2 d\Omega)$, V_{bin} : radar resolution volume

Radar equation for volume scattering

$$\int_{V} \frac{\left|f_{n}(\theta,\varphi)\right|^{4}}{r^{2}} d\Omega \cong \frac{1}{r^{2}} \frac{\pi \Theta_{3dB} \Phi_{3dB}}{8 \ln 2} \quad (\text{Probert - Jones correction})$$

$$\langle W_R \rangle = \left(\frac{W_T G_M^2 \lambda^2}{(4\pi)^3}\right) L^2 \eta \Delta r \frac{1}{r^2} \frac{\pi \Theta_{3dB} \Phi_{3dB}}{8 \ln 2} \qquad \Longrightarrow \qquad \langle W_R \rangle = C_2 L^2 \frac{\eta}{r^2}$$



bin

RADAR SIGNAL Signal fluctuations

Power fluctuations of radar echo

Complex envelope due to i-th scatterer:

$$V_i(t) = A_i e^{j\varphi_i(t)}, \quad \varphi_i(t) = -4\pi r_i(t) / \lambda + \psi_i$$

• Total complex envelope due to distributed scatterers:

$$V(t) = I(t) + jQ(t) = \sum_{i} V_{i}(t) = \sum_{i} A_{i}e^{j\varphi_{i}(t)} = A(t)e^{j\varphi(t)}$$

In-phase and quadrature components

$$\begin{cases} I(t) = \operatorname{Re}[V(t)] = A(t)\cos\varphi(t) \\ Q(t) = \operatorname{Im}[V(t)] = A(t)\sin\varphi(t) \end{cases} \text{ with } A = \sqrt{I^2 + Q^2}, \varphi = \operatorname{artg} \frac{Q}{I} \end{cases}$$

Radar echo power

$$W_{R}(t) = kV(t)V(t)^{*} = A^{2}(t) = k\sum_{i}A_{i}^{2} + k\sum_{i\neq j}A_{i}A_{j}e^{j(-4\pi/\lambda)(r_{i}-r_{j})} = \begin{cases} W_{Rdc} + W_{Rac} \\ < W_{R} > +\widetilde{W}_{R} \end{cases}$$

- From one pulse to next, power fluctuation W_{ac} are related to scatterer random • displacement (velocity or Doppler frequency).
- It results <W_{ac}>=0 and W_{ac} decreases doing averages on independent samples (such that displacement > λ). For estimating ΔΦ, samples must be correlated to avoid ambiguity.

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RADAR SIGNAL Statistics of power fluctuations

Distribution of I, Q

- For the central limit, V(t) is Gaussian so that I and Q
- A and Φ are independent random variables with Φ uniformly distributed in 0-2 π .

$$p(I,Q) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-(I^2 + Q^2)/2\sigma^2}, \quad p(I,Q)dIdQ = p(A,\varphi)dAd\varphi, \quad dIdQ = AdAd\varphi$$

Marginal distribution of A, φ

$$p(A,\varphi) = \frac{A}{\sqrt{2\pi\sigma^2}} e^{-A/2\sigma^2} \implies \begin{cases} p(A) = \frac{A}{\sqrt{2\pi\sigma^2}} e^{-A/2\sigma^2} & \text{Rayleigh pdf} \\ p(\varphi) = 1/2\pi & \text{Uniform pdf} \end{cases}$$

Square-law detector statistics of received power

$$W_R = A^2$$
, $dW_R = 2AdA$, $p(W_R)dW_R = p(A)dA \implies p(W_R) = \frac{1}{2\sigma^2}e^{-W_R/2\sigma^2}$ Exponential pdf

RADAR SIGNAL Decorrelation time

Dopppler spectrum

- Duration t_d needed to ensure sample independence depends on volume and wavelength
- Doppler spectrum is of Gaussian type for uniform regions:

$$p(f_d) = p_0 e^{-f_d^2 / 2\sigma_f^2}; \quad f_d = (2/\lambda)u_r$$

Time autocorrelation function:

$$R(t_d) = R_0 e^{-t_d^2/2\sigma_t^2}, \sigma_t = \frac{1}{2\pi\sigma_f} = \frac{1}{2\pi(2/\lambda)\sigma_u}$$

Decorrelation time t_{inc}

$$R(t_{inc})/R_0 = 0.02 \implies t_{inc} = 2\lambda/\sigma_v$$



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Snow:
$$\sigma_u = 0.5 \text{ m/s}$$

Rain: $\sigma_u = 1 \text{ m/s}$

RADAR SIGNAL Time-space data integration

Signal variance reduction

- For meteorological appliatio, W_{dc} is of interest so that W_{ac} must be reduced
- How many independent samples of received power must be averaged to accurately estimate W_{dc}=<W> using a square-law detector?

$$J_k = \frac{1}{k} \sum_{n=1}^k W_{Rn}$$
 with $p(J_k) dJ_k = p(A_n^2) d(A_n^2)$

- The final pdf is almost Gaussian for k>10
- For k=30, <W> error estimate is about 1 dB

Spatial integration

- For fast scannig, spatial averaging is performed together with time integration
- Reduction of measurement spatial resolution (e.g., range similar to transverse)



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- Operational problem overview
- Clouds and precipitation
- Rainfall backscattering and polarimetric measurables
- Example of radar measurements and estimates

RADAR APPLICATIONS Clouds and precipitation

Genus	Sym.	Region	Species	RR (mm/h)		
Cumulus	Cu	Vert. develop. (0-6 Km)	Mediocris Congestus Incus	0 < 30 < 60	Cirriform Stratiform Cumuliform	
Cumulonimbus	Cb	Vert. develop. (0-12 km)		10÷100	High Ci Cs Cr Charles	-
Stratus	St	low (0-2 km)		< 2		
Stratocumulus	Sc	low (0-2 km)		< 5		ł
Nimbostratus	Ns	middle (2-6 km)		< 15		1
Altostratus	As	middle (2-6 Km)		< 2	Middle Ms totujount	4
Altocumulus	Ac	middle (2-6 km)		0		Ľ
Cirrostratus	Cs	high (6-12 km)		0	<u>St</u>	
Cirrocumulus	Cc	high (6-12 km)		0	LOW	2 1 4

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DYNAMIC METEOROLOGY Air mass flows and winds



DYNAMIC METEOROLOGY Circulating cells







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DYNAMIC METEOROLOGY Cyclones and anticyclones







CLOUD GENERA Warm fronts



CLOUD GENERA Cold fronts



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CLOUD FRONTS Cold, warm and occluded



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PRECIPITATING CLOUDS Time and space scales

		CHA			
		1 day- 1 month	1 hour – 1 day	1 hour – 1 minute	
	200 - 2000 km	- Fronts			Meso-α scale
		- Hurricanes			
Η		(tens of days)			
0	20 - 200 km		- Squall lines		Meso-ß scale
R			- Cloud clusters		
Ι			- Mountain and		
Ζ			lake disturbances		
0			(2 hours to 1 day)		
Ν	2 - 20 km			- Thunderstorms	Meso-y scale
Т				(tens of minutes to	•
Α				hours)	
L	0.2 - 2 km			- Tornadoes	Micro-a scale
				- Deep convection	
~				(few minutes to 1	
S				hour)	
C	0.02 - 0.2 km			- Thermals	Micro-B scale
A				(few minutes)	•
	0.001 - 0.02 km			- Plumes	Micro-y scale
F				- Turbulence	
				(less than a	
				few minutes)	

PRECIPITATING CLOUDS Stratiform process



PRECIPITATING CLOUDS Ice crystals

As for droplets (condensation/evaporation), ice crystals can initially grow by *vapor deposition* and evaporate by *sublimation*. The probability of presence of ice particles in a cloud increases with decreasing temperature below zero. At -10°C the probability to find ice is around 50%, while at -20 °C it raises to 95%.

Main ice crystal shapes are: (a) columnar or prismatic, (b) disc, (c) dendrite



PRECIPITATING CLOUDS Convective process



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PRECIPITATING CLOUDS Graupel particles

GRAUPEL FORMATION BY RIMING

•Ice crystals fall through supercooled cloud droplets

•Supercooled droplets, that hit ice crystals, freeze to it

•Eventually the frozen droplet can hide the original shape

•Due to strong updrafts, hailstones can form

	Rimed crysta	Hexagona graupel	l Conelike graupel	
		a ¹	a2 (100)	°3 🕼
	Plane crystal	b ₁ Break off		^{b2}
Without tumbling (rotation)		^{c1}		^c ²
	Columnar crystal	d		d2 00 x
	Radiating assemblage of plane branches	۳ 💥		*² 🕼
	Frozen drop	f1		¹ 2
	Rimed crysto	L	Lump graupel	
With tumbling (rotation)	Columnar crystal	91	92	
	Radiating assemblage of plane branches	h _i	. h ₂	۰ 🛞
	Frozen drop	ⁱ 1 🐐	12	•

Natural graupels (boxes are 2 mm on a side)



RADAR APPLICATIONS Drop size distributions

Modified Gamma distribution

 $N(D) = N_0 D^{\mu} e^{-\Lambda D}$

Moments of order n:

$$m_n = \int_0^\infty D^n N(D) dD = \frac{N_0 \Gamma(n + \mu + 1)}{\Lambda^{n + \mu + 1}}$$
$$N_T = m_0$$

with D: drop diameter; N_0, μ, Λ : parameters

- Drop concentration [#/m³]:
- Equivalent water content [g/m³]: $M = (\pi/6)\rho m_3$
- Median volumetric diameter [m]: $D_0 = M/2$
- Precipitation intensity [mm/h]: $R_{\rho} = (\pi/6)\rho \int D^3 N(D)[u_t(D) w] dD$ [kg/m²s]

 $u_t(D) = aD^b \implies R = R_\rho / \rho = (\pi/6)am_{3+b} \text{ [m/s = mm/h]}$

RADAR APPLICATIONS Examples of size distributions



RADAR APPLICATIONS Atmospheric attenuation

$$\alpha = k_a = 0.4343 \int_{0}^{\infty} \sigma_a(D) N(D) dD \text{ [dB/km]} \Rightarrow$$



 α_{g} : atmospheric gases α_{c} : cloud and ice α_{p} : rain and graupel (precipitating) $\alpha_{t} = \alpha_{g} + \alpha_{c} + \alpha_{p}$ $a_{p} = \kappa_{p}\kappa$



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RADAR APPLICATIONS Radar reflectivity

Volumetric reflectivity of particles with different size

$$\eta = \frac{\sum_{i=1}^{N_{part}} \sigma_{bi}}{dV} \rightarrow \frac{\sum_{i=1}^{N_{p}} \sigma_{b}(D_{i}) N_{p}(D_{i})}{dV} = \sum_{i=1}^{N_{p}} \sigma_{b}(D_{i}) N(D_{i}) \cong \int_{0}^{\infty} \sigma_{b}(D) N(D) dD \quad \left[\frac{1}{m}\right]$$

Rayleigh reflectivity and reflectivity factor

•

Se D <<
$$\lambda$$
: $\eta = \int_{0}^{\infty} \left[\frac{\pi^{5} |K|^{2}}{\lambda^{4}} D^{6} \right] N(D) dD \implies Z \equiv \int_{0}^{\infty} D^{6} N(D) dD$

Mie reflectivity and equivalent reflectivity factor

$$Se D > \lambda: \quad \eta = \frac{\pi^5 |K|^2}{\lambda^4} Z_e \implies Z_e \equiv \frac{\lambda^4}{\pi^5 |K|^2} \int_0^\infty \sigma_b(D) N(D) dD$$

Dielectric factor K Water $|K|^2 = 0.930$
Ice $|K|^2 = 0.176$
Melt $|K|^2 = 0.208$

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RADAR APPLICATIONS Examples of radar reflectivity



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Power-law relation: $Z=aR^b$

RADAR APPLICATIONS Hydrologic relationships

Parameter	Stratiform [Marshall and Palmer, 1948]	Thunderstorm [Sekhon and Srivastava, 1971]	Snow [Sekhon and Srivastava, 1970]
Z-R	$Z = 200 R^{1.6}$	$Z = 300 R^{1.35}$	$Z = 1780 R^{2.21}$
M-R	$M = 0.072 R^{0.88}$	$M = 0.052 R^{0.94}$	$M = 0.250 R^{0.86}$
D ₀ -R	$D_0 = 0.09 R^{0.21}$	$D_0 = 0.13 R^{0.14}$	$D_0 = 0.14 R^{0.45}$
Γ-R	$\Gamma = 41 R^{-0.21}$	$\Gamma = 38 R^{-0.14}$	$\Gamma = 22.9 R^{-0.45}$
N ₀ -R	$N_0 = 0.08$	$N_0 = 0.07 R^{0.37}$	$N_0 = 0.025 R^{-0.94}$
Γ-M	$\Gamma = 22 M^{-0.24}$	$\Gamma = 25 M^{-0.15}$	$\Gamma = 11 M^{-0.52}$

Note:

Z is in mm⁶ m⁻³, R is in mm h⁻¹, M is in g m⁻³ m⁻³, D_0 is in cm, Γ is in cm⁻¹, N_0 is in cm⁻⁴.

RADAR APPLICATIONS Polarized measurements

Backscattering matrix

• The scattering field is related to the incident one by:

$$\begin{bmatrix} E_h^{s} \\ E_v^{s} \end{bmatrix} = \frac{e^{-j\beta r}}{r} \begin{bmatrix} S_{HH} & S_{HV} \\ S_{VH} & S_{VV} \end{bmatrix} \begin{bmatrix} E_h^{i} \\ E_v^{i} \end{bmatrix}$$

• The S matrix is the complex backscattering matrix, whose terms are:

$$S_{pp} = \left| S_{pp} \right| e^{j\varphi_{pp}}$$

Interpretation and Symmetry

- Diagonal terms S_{HH} and S_{VV} represent linear co-polarized components
 S_{HH} : H transmission, H reception
- Off-diagonal terms are cross-polarized components
 S_{VH}: H transmission, V reception
- For a spherical particles, the cross-polarized terms are zero.
- The cross-pol. terms are equal for reciprocity (unless medium is anysotropic).





RADAR APPLICATIONS Polarimetric definitions

Polarimetric form of radar equation

- Radar equation can be generalized to polarimetric form
- Complex envelope V will be polarization dependent, i.e. V_{pp}
- Co-polar radar reflectivity (mm⁶m⁻³)

$$Z_{HH} = (\lambda^4 / \pi^5 |K|^2) < |S_{HH}|^2 >, \quad Z_{VV} = (\lambda^4 / \pi^5 |K|^2) < |S_{VV}|^2 >$$

Differential reflectivity

$$Z_{DR} = 10 Log \frac{<|S_{HH}|^2>}{<|S_{VV}|^2>}$$

Linear Depolarization Ratio (LDR)

$$LDR = 10Log \frac{<|S_{HV}|^2 >}{<|S_{HH}|^2 >}$$



RADAR APPLICATIONS Polarimetric examples



$$Z_{DR} = 10 Log \frac{<|S_{HH}|^2 >}{<|S_{VV}|^2 >}$$

Oblate
$$\rightarrow Z_{DR} > 0$$

Sphere $\rightarrow Z_{DR} = 0$
Prolate $\rightarrow Z_{DR} < 0$



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RADAR APPLICATIONS Polarimetric definitions

Correlation coefficient

$$\rho_{HV} = \frac{\langle S_{VV} S_{HH}^* \rangle}{\sqrt{\langle |S_{HH}|^2 \rangle \langle |S_{VV}|^2 \rangle}} = |\rho_{hv}| e^{j\delta_{hv}}$$

Differential propagation-phase shift (°/km)

$$K_{DP} = \frac{180}{\pi} \lambda \operatorname{Re} \left[\int_{0}^{D} [f_{HH}(D) - f_{VV}(D)] N(D) dD \right]$$

$$\phi_{DP} = 2 \int_{0}^{r} K_{DP}(r') dr' + \delta_{hv}$$

$$\delta_{hv} = \operatorname{arg} \left(< S_{VV} S_{HH}^{*} > \right)$$

- Oblate particles tend to slow down **H-pol**. waves with respect to **V-pol**. ones
- This effect is larger for liquid than ice particles
- δ is due to particle-induced phase shift

RADAR APPLICATIONS Polarimetric definitions

Specific attenuation (1/km)

$$\alpha_{HH} = 2 \cdot 10^{-3} \frac{180}{\pi} \lambda \,\mathrm{Im} \Big[< 4\pi S_{HH}^{f} (D_{e}, \phi) > \Big]$$

One-way path attenuation

$$A_{HH}(r) = \int_{0}^{r} \alpha_{HH}(r') dr'$$

$$A_{HH}(r) = \int_{0}^{r} \alpha_{HH}(r') dr'$$

$$W_{Rh} \ge C_{2}L_{HH}^{2}(r) \frac{Z_{HH}(r)}{r^{2}} =$$

$$= C_{2} \left(e^{-2A_{HH}(r)}\right) \frac{Z_{HH}(r)}{r^{2}}$$

$$A_{Renuation of backscattered power (due to a range bin) along the path of backscattered power$$

RADAR APPLICATIONS Polarimetric theory



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RADAR APPLICATIONS Polarimetric features

Table 1. Values of polarimetric variables for precipitation types (from Doviak and Zrnić 1993).

	Z_{h} (dBZ)	Z_{DR} (dB)	$ ho_{hv}$	K _{DP} (° km ⁻¹)	LDR (dB)
Drizzle	< 25	0	>0.99	0	<-34
Rain	25 to 60	.5 to 4	>0.97	0 to 10	-27 to -34
Dry snow	< 35	0 to .5	>0.99	0 to 0.5	<-34
Dense snow	< 25	0 to 5	>0.95	0 to 1	-25 to -34
Wet snow	< 45	0 to 3	0.8 to 0.95	0 to 2	-13 to -18
Dry graupel	40 to 50	-0.5 to 1	>0.99	-0.5 to 0.5	< -30
Wet graupel	40 to 55	-0.5 to 3	>0.99	-0.5 to 2	-20 to -25
Wet hail (< 2 cm)	50 to 60	-0.5 to 0.5	>0.95	-0.5 to 0.5	<-20
Wet hail (> 2 cm)	55 to 70	<-0.5	>0.96	-1 to 1	-10 to -15
Rain/hail	50 to 70	-1 to 1	>0.90	0 to 10	-10 to -20

RADAR APPLICATIONS Polarimetric advantages

TABLE 1. Attributes of polarimetric variables (for 5- and 10-cm wavelengths).

Attribute Variable	Independent of absolute radar	Immune to propagation effects calibration	Immune to noise bias	Used for quantitative estimation	Independent of concen- tration
Z_k^{-}	no	no	no	yes	no
Z_{DR}	yes	no	no	yes	yes
$K_{_{DP}}$	yes	yes	yes	yes	no
$\rho_{_{hv}}$	yes	yes	no	no	yes
δ	yes	no	yes	no	yes
LDR	yes	no	no	no	yes
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RADAR APPLICATIONS Rainfall polarimetric estimators



From single-pol. $R = R(Z_h, Z_{dr})$

To dual-pol. retrieval

$$R = R(Z_h, Z_{dr})$$
$$R = R(K_{dp}, Z_{dr})$$
$$R = R(K_{dp})$$

RADAR APPLICATION Measurement issues

Volume **Dual-pol. radar equation** h bin $\langle W_{Rh,v}(r,\theta,\phi) \rangle = \frac{1}{M_{nulse}} \sum_{i=1}^{M_{pulse}} W_{iRh,v}(r,\theta,\phi) - N_R$ $Z_{xx}(r,\theta,\varphi)$ $Z_{HH,VV}(r,\theta,\phi) = C_2 r^2 < W_{Rh,v} > (r,\theta,\phi) e^{2A_{HH,VV}(r,\theta,\phi)}$ Ground clutter where $P_{\rm R}$: received power at h or v pol. C: radar constant, r: range A: path attenuation at h or v pol. *Z*: reflectivity at *h*-*h* or *v*-*v* pol. N_{R} : noise level M: number of pulses Radar V pol $\mathbf{Z}_{\mathbf{surf}}(h)$ Path Н attenuation H pol

RADAR APPLICATIONS Operational issues

Calibration objective

- Determine with precision and accuracy the instrumental constant C in radar equation equation
 - Transmistter power, loss of radiofrequency chain (e.g., guides, mixers, couplers)
 - Noise level in the receiver chain, receiver gain and linear dynamics (no distortions)

Calibration techniques

- Internal calibration: measurement of each radar component and module
 - Suitable instrumentation (e.g., synthetic pulse generator, network analyzer)
 - Periodic controls (antenna, TX) vs. frequent controls (oscillators, noise)
- External calibration: measurement of reference radar targets
 - Large metallic spheres such that σ_{b} is equal to the geometric section
 - Rain-gauge time-series data
 - Difficult measurement set up and ambiguities
- Overall calibration obtainable: ≥1 dB

Ground-clutter contamination

- Spurious echoes backscattered by ground and obstacles
- Spectral, statistical and static removal techniques
- Coupling with beam occulation, anomalous propagation, reflectivity gradients

RADAR PRODUCTS An overview





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RADAR PRODUCTS Comparison among instruments

Rain gauges



Meteosat IR



RADAR PRODUCTS Comparison among instruments

Meteosat IR

C-band Radar (ARPA-FVG)



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RADAR PRODUCTS Comparison among instruments



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RADAR PRODUCTS Polar volume scanning



SCANNING STRATEGY Elevation angle θ : 0-20 with variable step Azimuth angle ϕ : 0-360° with 1° step



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RADAR PRODUCTS Plan Position Indicator (PPI)

Projection on the ground plane of radar 3-D polar data acquired upon a conical surface (constant elevation, azimuth betwen 0° and 360°)



RADAR PRODUCTS Example of PPI

H-pol. Reflectivity at 2^{\circ} elevation



Radial velocity at 2° elevation



RADAR PRODUCTS Range Height Indicator (RHI)

RHI: Vertical scan for constant azimuth angle φ



RADAR PRODUCTS Example of RHI and VCut



RADAR PRODUCTS Constant Altitude PPI

CAPPI: Horizontal cut of polar volume at a constant altitude



RADAR PRODUCTS CAPPI processing



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RADAR PRODUCTS Example of CAPPI



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RADAR PRODUCTS Hor.-Vertical Maximu Intensity

HVMI: Horizontal-vertical projection (3 axes) of maximum reflectivity



RADAR PRODUCTS Example of VMI



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RADAR PRODUCTS Errors in rainfall retrieval

- 1. Inhomogenheity of rain cloud within the radar beam
- 2. Evaporation of rainfall below the radar beam

3. Understimation due to orographic effects on rainfall process

4. Bright-band effects due to melting layer

5. Path attenuation due clear-air gases (water vapor and oxygen) and rain

6. Anamolous propagation due to air refractivity – second-trip echoes

7. Beam screening due to presence of obastacles (hills, mountains)

8. Calibration erros within the radar system





RADAR PRODUCTS Examples of radar artifacts (1)



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RADAR PRODUCTS Examples of radar artifacts (2)



Estimate of surface rainfall from stratiform or convective Z-R relation ?



RADAR PRODUCTS Examples of radar artifacts (3)

Max. unamb. velocoty: $u_{max} = \pm 16$ m/s Mode: single PRF=1180 Hz

Max. unamb. velocoty: $u_{max} = \pm 32m/s$ Mode: dual PRF=1180 Hz, 787 Hz



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S-band radar: immune to rain path attenuation



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RADAR PRODUCTS Radar data processing



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RADAR PRODUCTS Example of data processing



RADAR PRODUCTS Surface rainfall C-band retrieval



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RADAR PRODUCTS Retrieval expected accuracy



 $\left\langle \left[\hat{R}_{est} - R_{sim} \right]^{2} \right\rangle$ FSE =Algorithms: $R_1 = M - P$ R₂=WSR-88D $R_{dp} = G.$ et al. (rob) $R_1(K_{dp}) = S - Z$ $R_2(K_{dp})=G-S$ (lin)

RADAR PRODUCTS Path attenuation mitigation

S-band radar: immune to rain path attenuation

C-band radar: corrected for rain path attenuation using fully polarimetric data (Zh, Zdr, Kdp)



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RADAR PRODUCTS Hydrometeor classification

Hailstorm in Florida observed by Sband polarimetric radar

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Ditterential Reflectivity (dB)



... and derived hydrometeor classification

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